

On the expressivity of the Mobile Ambients and the π -calculus

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AMAST, 23-25 June 2010 - Quebec city

Outline

Introduction
The two languages
Our encoding
Conclusions
Future work

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Divergence seems to be the intrinsic distance between MA and π .

The syntax of Mobile Ambients

We consider the pure Mobile Ambients, with recursion.

$$\begin{aligned} P &::= \mathbf{0} \mid X \mid M.P \mid (\nu n)P \mid P|P' \mid \mu X.P \mid n[P] \\ M &::= in\ n \mid out\ n \mid open\ n \end{aligned}$$

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$$\mu X.P \equiv P[\mu X.P/X], \text{ up to } \alpha\text{-conversion}$$

The operational semantics of Mobile Ambients

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$P' \equiv P, P \rightarrow Q, Q \equiv Q' \Rightarrow P' \rightarrow Q'$	\equiv

The syntax of π -calculus

A polyadic version, with process identifiers:

$$Q ::= \mathbf{0} \mid \pi.Q \mid (\nu a)Q \mid Q|Q' \mid Q + Q' \mid$$

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$$\frac{P \xrightarrow{\bar{a}(\tilde{b})} P', Q \xrightarrow{a(\tilde{x})} Q'}{P|Q \xrightarrow{(\bar{a}(\tilde{b}), a(\tilde{x}))} (\nu \tilde{b})(P'|Q'[\tilde{b}/\tilde{x}])} \text{ (bound com)}$$

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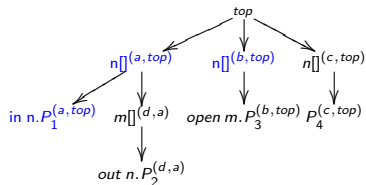
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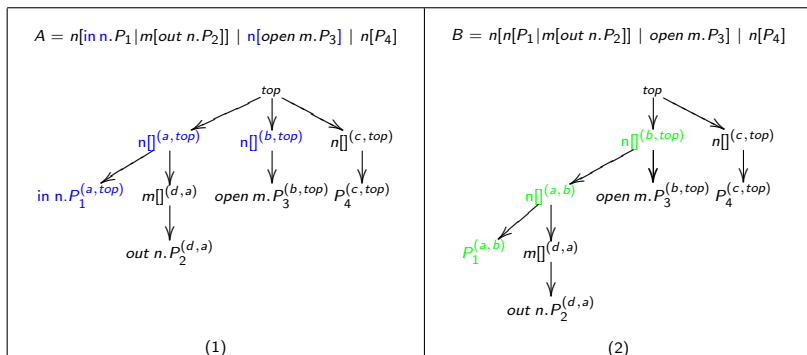
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- ▶ **top** identifies the topmost ambient

The basic dynamics

$$A = n[\text{in } n.P_1 \mid m[\text{out } n.P_2]] \mid n[\text{open } m.P_3] \mid n[P_4]$$


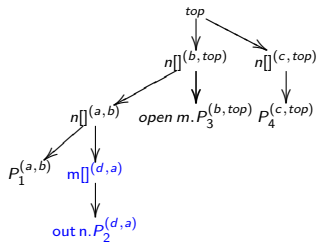
(1)

The basic dynamics



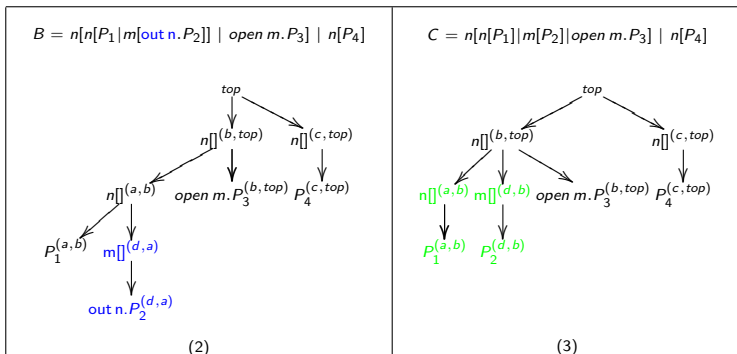
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$$B = n[n[P_1 | m[\text{out } n.P_2]] | \text{open } m.P_3] | n[P_4]$$

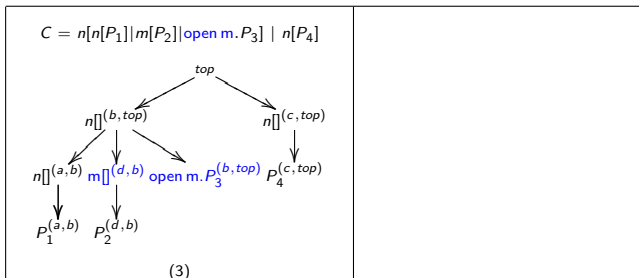


(2)

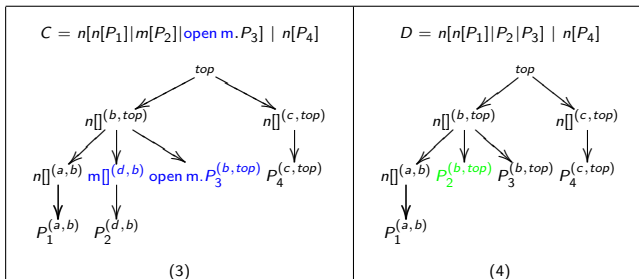
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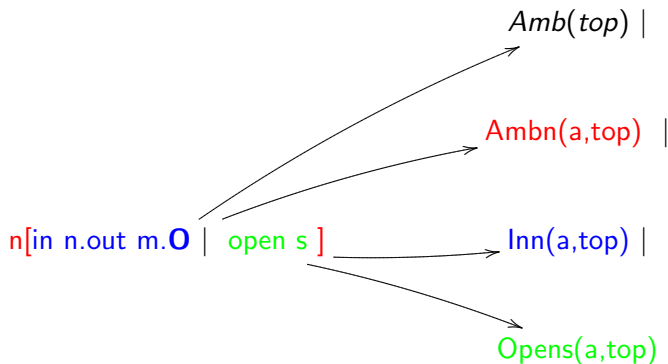
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The basic idea



Main encoding function

$$\mathcal{T} : \mathcal{P}_{MA} \times \mathcal{N} \rightarrow \mathcal{P}_{\pi}$$

$$\mathcal{T}(P, top) = (\nu \tilde{m})\mathcal{T}_a(P, top, top) | \text{Amb}(top)$$

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where:

- ▶ $\tilde{m} = fn(\mathcal{T}_a(P, top, top))$,
- ▶ $\mathcal{T}_a : \mathcal{P}_{MA} \times \mathcal{N} \times \mathcal{N} \rightarrow \mathcal{P}_\pi$

An example

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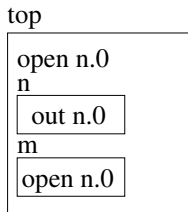
$$\begin{aligned}
 T(P, \text{top}) \equiv Q &= (\nu \text{ top}, a, b, \dots) \\
 &\quad \text{Amb}(\text{top}) | \text{Openn}(\text{top}, \text{top}) \\
 &\quad | \text{Ambn}(a, \text{top}) | \text{Outn}(a, \text{top}) \\
 &\quad | \text{Ambm}(b, \text{top}) | \text{Openn}(b, \text{top})
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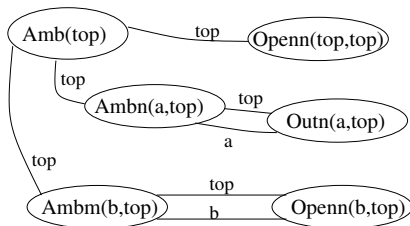
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Mobile Ambients



π -Calculus



Encoding processes at work

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Mimicking a capability:

$$\begin{aligned} \mathcal{T}(P, \text{top}) \xrightarrow{\tilde{\theta}}^* Q' &\equiv \text{Amb}(\text{top}) \\ &| \text{Opened}(a, \text{top}, \text{top}) | \text{Outn}(a, \text{top}) \\ &| \text{Ambm}(m', \text{top}) | \text{Openn}(m', \text{top}) \end{aligned}$$

Acting as a link

The code:

$$\begin{aligned} \textit{Opened}(a, a', f') &= a(x).\bar{x}\langle a', f' \rangle.\textit{Opened}(a, a', f') \\ &+ \\ &a(x, x').\bar{x}\langle a', f' \rangle.\textit{Opened}(a, a', f') \end{aligned}$$

Running *encoding processes*

$$\mathcal{T}(P, \text{top}) = Q \xrightarrow{\theta} Q' \equiv (\nu \text{top}, a, \dots) \text{Amb}(\text{top}) | \text{Opened}(a, \text{top}, \text{top}) | \text{Outn}(a, \text{top}) | \text{Ambm}(m', \text{top}) | \text{Openn}(m', \text{top})$$

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- ▶ Process $\text{Opened}(a, \text{top}, \text{top})$ has substituted the dissolved $\text{Ambn}(a, \text{top})$.
- ▶ The old coordinates will be updated as soon as $\text{Outn}(a, \text{top})$ will try to mimic the ‘out n’ capability.

$\text{Opened}(a, \text{top}, \text{top})$ only acts as a link between the old channel name **a** of the dissolved ambient, and the unique channel name **top** associated to the ambient which has taken its place.

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$$\mathcal{T}(P', \text{top}) = Q'' \equiv (\nu \text{top}, b, \dots) \text{Amb}(\text{top}) | \text{Outn}(\text{top}, \text{top}) | \text{Ambm}(b, \text{top}) | \text{Openn}(b, \text{top})$$

Encoding processes at work

Now we have that:

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$$\begin{aligned} T(P', \text{top}) = Q'' &\equiv (\nu \text{ top}, b) \text{Amb}(\text{top}) \\ &| \text{Outn}(\text{top}, \text{top}) \\ &| \text{Ambm}(b, \text{top}) | \text{Openn}(b, \text{top}) \end{aligned}$$

Q' differs from Q'' as it contains the subprocess $\text{Opened}(a, \text{top}, \text{top})$ and different coordinates for $\text{Outn}(a, \text{top})$.

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 - ▶ i.e. those processes that differs from $A\pi$ because may contain *Opened()* subprocesses.

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The notions of traces

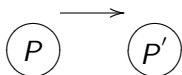
A capability execution in MA: $P \rightarrow P'$

A capability mimicking in π -calculus:

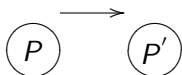
$$\mathcal{T}(P, \text{top}) \xrightarrow{\theta_1} \dots \xrightarrow{\theta_n} Q'$$

- ▶ Q' records the effects of a capability simulation, $\xi = \theta_1 \dots \theta_n$ is a *simulating trace*
- ▶ if $Q' \equiv \mathcal{T}(P, \text{top})$ then we have an *aborting trace*

The simulation of a capability

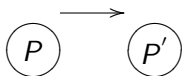


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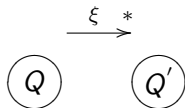


Simulating trace: ξ

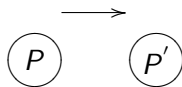
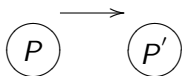
The simulation of a capability



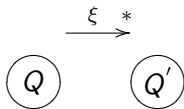
Simulating trace: ξ



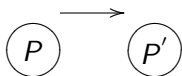
The simulation of a capability



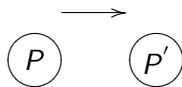
Simulating trace: ξ



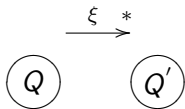
The simulation of a capability



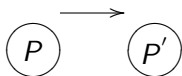
Simulating trace: ξ



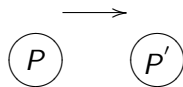
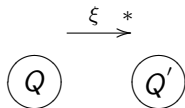
Aborting trace: ξ



The simulation of a capability



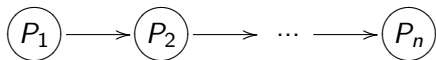
Simulating trace: ξ



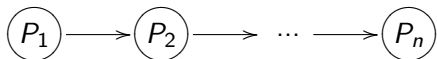
Aborting trace: ξ



Ordered execution of traces

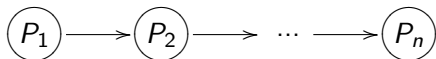


Ordered execution of traces

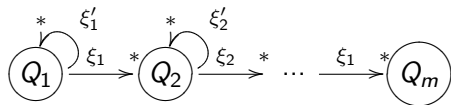


Assuming to execute orderly a trace per time.

Ordered execution of traces



Assuming to execute orderly a trace per time.



Weak soundness

Let P be a MA process,

if $\mathcal{T}(P, \text{top}) = Q \xrightarrow{\tilde{\theta}_a^*} Q'$, then $\exists P', Q''$ such that $Q' \xrightarrow{\tilde{\theta}_b^*} Q''$,
 $Q'' \simeq \mathcal{T}(P', \text{top})$ with $P \rightarrow^* P'$.

Completeness

Let P be a MA process, if $P \rightarrow^* P'$ then there exists a process Q' such that $\mathcal{T}(P, top) \xrightarrow{\tilde{\theta}^*} Q'$ and $\mathcal{T}(P', top) \simeq Q'$.

Who I am - Where I am

A clear separation of the two information.

Who I am - Where I am

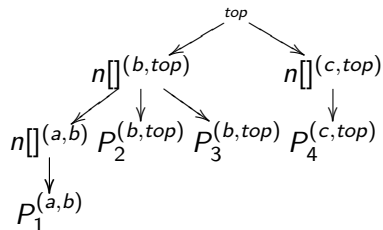
A clear separation of the two information.

$$D = n[n[P_1]|P_2|P_3] \mid n[P_4]$$

Who I am - Where I am

A clear separation of the two information.

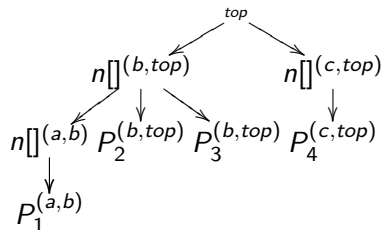
$$D = n[n[P_1]|P_2|P_3] | n[P_4]$$



Who I am - Where I am

A clear separation of the two information.

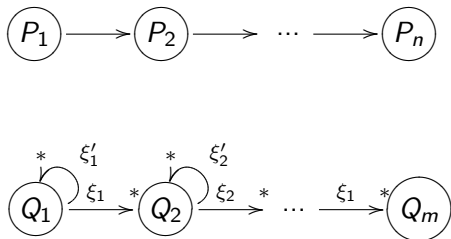
$$D = n[n[P_1] | P_2 | P_3] | n[P_4]$$



The ambient construct delimits a computing environment, and also holds a precise position within a hierarchical structure, hence each ambient has a unique 'address'.

The two transition systems

A clear relation between the two transition systems.



Behavioral characterization and LTL for MA

- ▶ A more elegant characterization between the two languages in terms of a behavioral equivalence, for example the testing equivalence.
- ▶ The understanding of the two roles of the ambients (Who-I-am,Where-I-am) could help in defining a simple LTL for MA.

Merci de votre attention

